

Homework 4

Complex numbers

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1.

$$\begin{aligned}z &= \frac{z_1}{z_2} \\ &= \frac{a + bi}{c + di} \\ &= \frac{i - 4}{2i - 3} \\ &= \frac{i - 4}{2i - 3} \cdot \frac{-3 - 2i}{-3 - 2i} \\ &= \frac{12 + 2 + (-3 + 8)i}{-3^2 + 2^2} \\ &= \frac{14 + 5i}{13}\end{aligned}$$

2.

$$\begin{aligned}(1 + i)^6 &= ((1 + i)(1 + i)^2)^2 \\ &= (2i(1 + i))^2 \\ &= (2(i - 1))^2 \\ &= 2^2(i - 1)^2 \\ &= 4 \cdot -2i \\ &= -8i\end{aligned}$$

This was not asked by the question, but I'd misread that part.

3. I had some problems doing these exercises, so I'd rather listen to your explanation tomorrow.

4. "

5. "

6. "

7. The multiply operation with a factor of 2 can be used. The wave now has an amplitude of 2; i.e. the wave oscillates between 2 and -2.

8. In that case, one could enter `2 * self` in the formula window.

9. `object[1] * object[2]`

`object["Sound sine"] * object["Sound cos"]`

10. The result of this multiplication is another sine wave.

$$\sin \alpha \cos \alpha = \frac{1}{2} \sin 2\alpha$$

So:

$$\sin(2\pi \cdot 377 \cdot t) \cos(2\pi \cdot 377 \cdot t) = \frac{1}{2} \sin(4\pi \cdot 754 \cdot 2t)$$